## Edexcel

## Pure Mathematics

Year 2

# Algebraic Methods 

Past paper questions from
Core Maths 3, Core Maths 4 and IAL C34


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1. Express

$$
\frac{2 x^{2}+3 x}{(2 x+3)(x-2)}-\frac{6}{x^{2}-x-2}
$$

as a single fraction in its simplest form.
2. (a) Simplify $\frac{3 x^{2}-x-2}{x^{2}-1}$.
(b) Hence, or otherwise, express $\frac{3 x^{2}-x-2}{x^{2}-1}-\frac{1}{x(x+1)}$ as a single fraction in its simplest form.
3. Given that

$$
\frac{2 x^{4}-3 x^{2}+x+1}{\left(x^{2}-1\right)} \equiv\left(a x^{2}+b x+c\right)+\frac{d x+e}{\left(x^{2}-1\right)}
$$

find the values of the constants $a, b, c, d$ and $e$.
4. The function $f$ is defined by

$$
\mathrm{f}: x \propto \frac{2(x-1)}{x^{2}-2 x-3}-\frac{1}{x-3}, x>3 .
$$

(a) Show that $f(x)=\frac{1}{x+1}, x>3$.
5.

$$
f(x)=\frac{2 x+2}{x^{2}-2 x-3}-\frac{x+1}{x-3}
$$

(a) Express $f(x)$ as a single fraction in its simplest form.
6. The function $f$ is defined by

$$
f(x)=1-\frac{2}{(x+4)}+\frac{x-8}{(x-2)(x+4)}, \quad x \in \mathbb{R}, x \neq-4, x \neq 2 .
$$

(a) Show that $\mathrm{f}(x)=\frac{x-3}{x-2}$.
7. Express

$$
\frac{x+1}{3 x^{2}-3}-\frac{1}{3 x+1}
$$

as a single fraction in its simplest form.
8. (a) Simplify fully

$$
\frac{2 x^{2}+9 x-5}{x^{2}+2 x-15}
$$

9. (a) Express

$$
\frac{4 x-1}{2(x-1)}-\frac{3}{2(x-1)(2 x-1)}
$$

as a single fraction in its simplest form.

Given that

$$
f(x)=\frac{4 x-1}{2(x-1)}-\frac{3}{2(x-1)(2 x-1)}-2, \quad x>1,
$$

(b) show that

$$
f(x)=\frac{3}{2 x-1} .
$$

10. 

$$
f(x)=\frac{4 x-5}{(2 x+1)(x-3)}-\frac{2 x}{x^{2}-9}, \quad x \neq \pm 3, x \neq-\frac{1}{2} .
$$

(a) Show that

$$
f(x)=\frac{5}{(2 x+1)(x-3)} .
$$

11. The function $f$ is defined by

$$
\mathrm{f}: x \propto \frac{3(x+1)}{2 x^{2}+7 x-4}-\frac{1}{x+4}, \quad x \in \mathbb{R}, x>\frac{1}{2} .
$$

(a) Show that $\mathrm{f}(x)=\frac{1}{2 x-1}$.
12. Express

$$
\frac{2(3 x+2)}{9 x^{2}-4}-\frac{2}{3 x+1}
$$

as a single fraction in its simplest form.
13.

$$
\mathrm{h}(x)=\frac{2}{x+2}+\frac{4}{x^{2}+5}-\frac{18}{\left(x^{2}+5\right)(x+2)}, \quad x \geq 0
$$

(a) Show that $\mathrm{h}(x)=\frac{2 x}{x^{2}+5}$.
(C3, Q7 Jan 2013)
14. Given that

$$
\frac{3 x^{4}-2 x^{3}-5 x^{2}-4}{x^{2}-4} \equiv a x^{2}+b x+c+\frac{d x+e}{x^{2}-4}, \quad x \neq \pm 2
$$

find the values of the constants $a, b, c, d$ and $e$.
15. Express

$$
\frac{3 x+5}{x^{2}+x-12}-\frac{2}{x-3}
$$

as a single fraction in its simplest form.
16.

$$
\mathrm{g}(x)=\frac{x}{x+3}+\frac{3(2 x+1)}{x^{2}+x-6}, \quad x>3
$$

(a) Show that $\mathrm{g}(x)=\frac{x+1}{x-2}, x>3$
17. Express

$$
\frac{3}{2 x+3}-\frac{1}{2 x-3}+\frac{6}{4 x^{2}-9}
$$

as a single fraction in its simplest form.
18.

$$
\mathrm{f}(x)=\frac{15}{3 x+4}-\frac{2 x}{x-1}+\frac{14}{(3 x+4)(x-1)}, \quad x>1
$$

(a) Express $\mathrm{f}(x)$ as a single fraction in its simplest form.
19. Given that

$$
4 x^{3}+2 x^{2}+17 x+8 \equiv(A x+B)\left(x^{2}+4\right)+C x+D
$$

(a) find the values of the constants $A, B, C$ and $D$.
20. Given that $k$ is a negative constant and that the function $\mathrm{f}(x)$ is defined by

$$
\mathrm{f}(x)=2-\frac{(x-5 k)(x-k)}{x^{2}-3 k x+2 k^{2}}, \quad x \geq 0
$$

(a) show that $\mathrm{f}(x)=\frac{x+k}{x-2 k}$.
(C3, Q9 June 2015)
21.

$$
\mathrm{f}(x)=\frac{x^{4}+x^{3}-3 x^{2}+7 x-6}{x^{2}+x-6}, \quad x>2, \quad x \in \mathbb{R} .
$$

(a) Given that

$$
\frac{x^{4}+x^{3}-3 x^{2}+7 x-6}{x^{2}+x-6} \equiv x^{2}+A+\frac{B}{x-2},
$$

find the values of the constants $A$ and $B$.
(C3, Q6 June 2016*)
22. Express $\frac{4 x}{x^{2} 9} \quad \frac{2}{x+3}$ as a single fraction in its simplest form.
(C3, Q1 June 2017)
23. The function f is defined by

$$
\mathrm{f}(x)=\frac{6}{2 x+5}+\frac{2}{2 x 5}+\frac{60}{4 x^{2} \quad 25}, \quad x>4
$$

Show that $\mathrm{f}(x)=\frac{A}{B x+C}$ where $A, B$ and $C$ are constants to be found.
24. Given that

$$
\frac{4 x^{3}-6 x^{2}-18 x+20}{x^{2}-4} \equiv a x+b+\frac{c}{x-2} \quad x \neq \pm 2
$$

find the values of the constants $a, b$ and $c$.
25.

Given that

$$
\frac{x^{4}+x^{3}-7 x^{2}+8 x-48}{x^{2}+x-12} \equiv x^{2}+A+\frac{B}{x-3}
$$

find the values of the constants $A$ and $B$.
(C34, Q3 June 2016_IAL)
26. (a) Express $\frac{5 x+3}{(2 x-3)(x+2)}$ in partial fractions.
(C4 June 2005 Q3)
27.

$$
\mathrm{f}(x)=\frac{3 x^{2}+16}{(1-3 x)(2+x)^{2}}=\frac{A}{(1-3 x)}+\frac{B}{(2+x)}+\frac{C}{(2+x)^{2}},|x|<\frac{1}{3} .
$$

(a) Find the values of $A$ and $C$ and show that $B=0$.
(C4 Jan 2006 Q5)
28.

$$
\mathrm{f}(x)=\frac{3 x-1}{(1-2 x)^{2}}, \quad|x|<\frac{1}{2} .
$$

Given that, for $x \neq \frac{1}{2}, \frac{3 x-1}{(1-2 x)^{2}}=\frac{A}{(1-2 x)}+\frac{B}{(1-2 x)^{2}}$, where $A$ and $B$ are constants,
(a) find the values of $A$ and $B$.
(C4 June 2006 Q2)
29.

$$
\frac{2\left(4 x^{2}+1\right)}{(2 x+1)(2 x-1)} \equiv A+\frac{B}{(2 x+1)}+\frac{C}{(2 x-1)} .
$$

(a) Find the values of the constants $A, B$ and $C$.
(C4 June 2007 Q4)
30.

$$
\mathrm{f}(x)=\frac{27 x^{2}+32 x+16}{(3 x+2)^{2}(1-x)},|x|<\frac{2}{3} .
$$

Given that $\mathrm{f}(x)$ can be expressed in the form

$$
\mathrm{f}(x)=\frac{A}{(3 x+2)}+\frac{B}{(3 x+2)^{2}}+\frac{C}{(1-x)},
$$

find the values of $B$ and $C$ and show that $A=0$.
31.

$$
\mathrm{f}(x)=\frac{4-2 x}{(2 x+1)(x+1)(x+3)}=\frac{A}{(2 x+1)}+\frac{B}{(x+1)}+\frac{C}{(x+3)} .
$$

(a) Find the values of the constants $A, B$ and $C$.
32.

$$
\frac{2 x^{2}+5 x-10}{(x-1)(x+2)} \equiv A+\frac{B}{x-1}+\frac{C}{x+2} .
$$

(a) Find the values of the constants $A, B$ and $C$.
(C4 June 2010 Q5)
33. (a) Express $\frac{5}{(x-1)(3 x+2)}$ in partial fractions.
(C4 Jan 2011 Q3)
34.

$$
\frac{9 x^{2}}{(x-1)^{2}(2 x+1)}=\frac{A}{(x-1)}+\frac{B}{(x-1)^{2}}+\frac{C}{(2 x+1)} .
$$

Find the values of the constants $A, B$ and $C$.
(C4 June 2011 Q1)
35. (a) Express $\frac{1}{P(5-P)}$ in partial fractions.
(C4 Jan 2012 Q8)
36.

$$
\mathrm{f}(x)=\frac{1}{x(3 x-1)^{2}}=\frac{A}{x}+\frac{B}{(3 x-1)}+\frac{C}{(3 x-1)^{2}} .
$$

(a) Find the values of the constants $A, B$ and $C$.
(C4 June 2012 Q1)
37. Express $\frac{9 x^{2}+20 x-10}{(x+2)(3 x-1)}$ in partial fractions.
38. Express in partial fractions

$$
\frac{5 x+3}{(2 x+1)(x+1)^{2}}
$$

39. (a) Express $\frac{25}{x^{2}(2 x+1)}$ in partial fractions.
(C4 June 2014_R Q4)
40. (a) Express $\frac{2}{P(P-2)}$ in partial fractions.
41. (a) Express $\frac{5-4 x}{(2 x-1)(x+1)}$ in partial fractions.
(IAL, C34 June 2014 Q6)
42. Given that

$$
\frac{4\left(x^{2}+6\right)}{(1-2 x)(2+x)^{2}} \equiv \frac{A}{(1-2 x)}+\frac{B}{(2+x)}+\frac{C}{(2+x)^{2}}
$$

(a) find the values of the constants $A$ and $C$ and show that $B=0$.
(IAL, C34 June 2015 Q2)
43. (a) Express $\frac{3 x^{2}-4}{x^{2}(3 x-2)}$ in partial fractions.
(IAL, C34 Jan 2016 Q9)
44. (a) Express $\frac{9+11 x}{(1-x)(3+2 x)}$ in partial fractions.
45.

$$
\begin{array}{c|cc}
6 & 5 x \quad 4 x^{2} \\
(2 & x)(1+2 x) & A+\frac{B}{(2 \quad x)}+\frac{C}{(1+2 x)}
\end{array}
$$

(a) Find the values of the constants $A, B$ and $C$.
46. (a) Express $\frac{9(4+x)}{169 x^{2}}$ in partial fractions.

